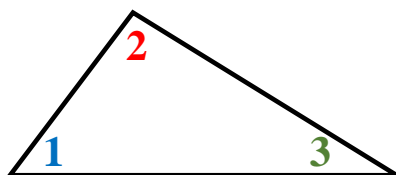
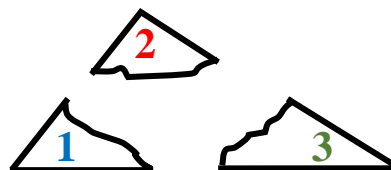


Prove that the interior angles of a triangle sum to 180° .



Alex's "Corner Tearing" Method

I ripped the corners off the triangle.



Then, I moved the pieces and saw that the angles create a straight line.

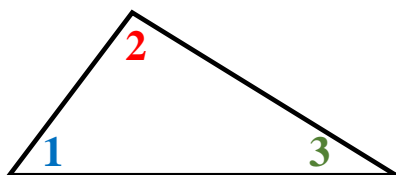


I already know a line is 180° , so the three angles of a triangle must add up to 180° .

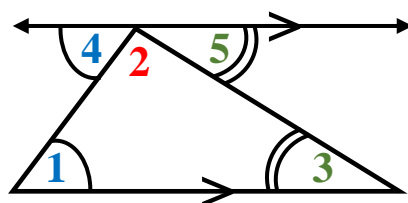
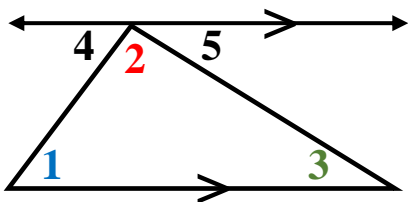
$$m\angle 1 + m\angle 2 + m\angle 3 = 180^\circ$$



Prove that the interior angles of a triangle sum to 180° .



Morgan's "Parallel Line" Method



$$m\angle 4 + m\angle 2 + m\angle 5 = 180^\circ$$

$$m\angle 1 + m\angle 2 + m\angle 3 = 180^\circ$$

I drew a line parallel to the bottom of the triangle, making $\angle 4$ and $\angle 5$.

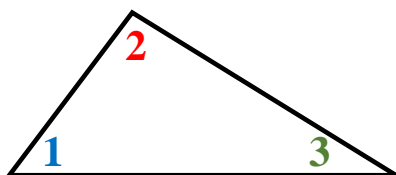
Because the lines are parallel,
 $m\angle 1 = m\angle 4$ and
 $m\angle 3 = m\angle 5$.

Angles 4, 2, and 5 make a straight line, and add to 180° .

Using substitution angles 1, 2, and 3 add to 180° .



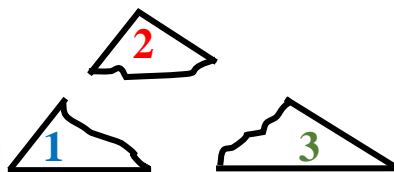
Prove that the interior angles of a triangle sum to 180° .



Alex's "Corner Tearing" Method

Morgan's "Parallel Line" Method

I ripped the corners off the triangle.



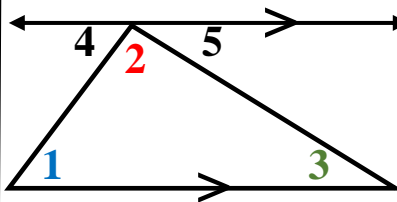
Then, I moved the pieces and saw that the angles create a straight line.



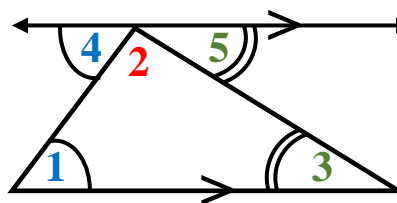
I already know a line is 180° , so the three angles of a triangle must add up to 180° .

$$m\angle 1 + m\angle 2 + m\angle 3 = 180^\circ$$

I drew a line parallel to the bottom of the triangle, making $\angle 4$ and $\angle 5$.



Because the lines are parallel, $m\angle 1 = m\angle 4$ and $m\angle 3 = m\angle 5$.



$$m\angle 4 + m\angle 2 + m\angle 5 = 180^\circ$$

Angles 4, 2, and 5 make a straight line, and add to 180° .

$$m\angle 1 + m\angle 2 + m\angle 3 = 180^\circ$$

Using substitution angles 1, 2, and 3 add to 180° .

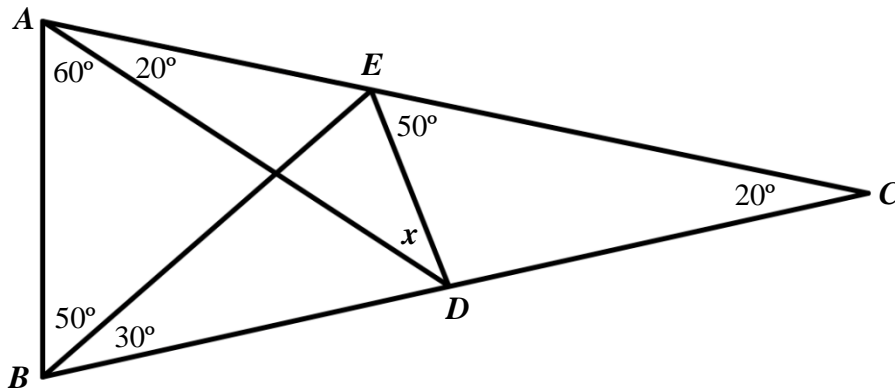


A.5: Triangle Angle Sum Theorem

1) What are the similarities and differences between Alex and Morgan's methods?

Similarities	Differences

2) Find the measure of angle x .



3) a) In Morgan's second step, why does she know that the $m\angle 1 = m\angle 4$ and $m\angle 3 = m\angle 5$?

b) Why was she able to use substitution in the fourth step?

4) What would Alex get if he tried his method on a quadrilateral?

Prove that the interior angles of a triangle add to 180° .

Alex's "Corner Toss"

I ripped the corners off the triangle.

Then, I moved the pieces and saw that the angles create a straight line.

I already know a straight line is 180° , so the three angles of a triangle must add up to 180° .

Wow! By looking at my method and Morgan's, I learned that the sum of the interior angles of a triangle will always add to 180° .

$$m\angle 1 + m\angle 2 + m\angle 3 = 180^\circ$$

$$m\angle 3 = 180^\circ$$

Using substitution angles 1, 2, and 3 add to 180° .

Angles 4, 2, and 5 make a straight line, and add to 180° .

Lines ℓ and ℓ' are parallel, $m\angle 4$ and $m\angle 5$ are alternate exterior angles, so $m\angle 4 = m\angle 5$.

